

# Comfort control in buildings using solar energy



UNED – Departamento de Informática y Automática  
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Área de Ingeniería de Sistemas y Automática



## Automatic control, Robotics and Mechatronics



2

**Modeling and control of solar plants**



**Modeling, control and robotics in agriculture**



**Energy efficiency and comfort control in buildings**



**Modeling and control of photobioreactors**



**Education in Engineering**

**Autonomous vehicles and robots**



**Design of robots**



**Vehicle dynamics**



**Vibration analysis**



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AUTOMÁTICA, ROBÓTICA Y MECATRÓNICA

ADVANCED CONTROL OF SOLAR PLANTS

Advances in Industrial Control

Springer

Control of Solar Energy Systems

AIC

Springer

CONTROL OF SOLAR ENERGY SYSTEMS

太阳能系统控制

太阳能发电系统控制技术

- **Modeling & Control of solar energy systems**



1. Tecnología de Receptor Central  
 2. Cilindro parabólicos con HTF  
 3. Cilindro parabólicos con GDV  
 4. Discos Parabólicos con motor Stirling  
 5. Concentrador Lineal tipo Fresnel

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Modeling and Control of Greenhouse Crop Growth

AIC

Springer

- **Control in agriculture**



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5

**• Solar energy and energy efficiency**





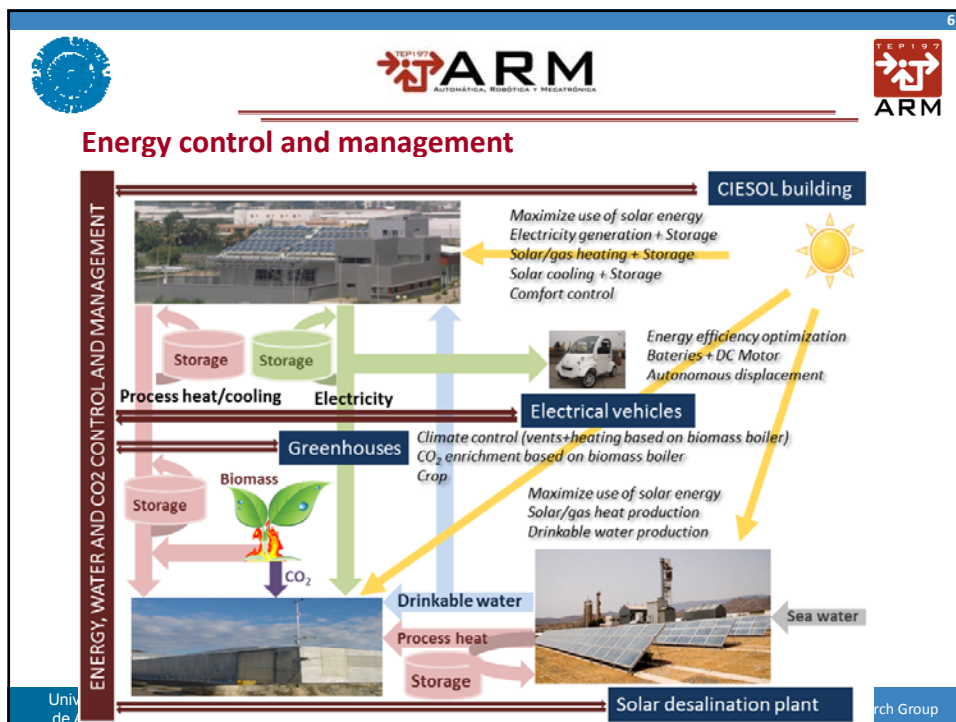







- Control of distributed collectors
- Solar cooling
- Comfort & energy control in buildings
- Other applications of solar energy

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## Disturbances forecast

Basic characteristics of solar radiation forecasting

Forecasting horizon:	Short-term	Long-term
Purpose (spatial nature):	Local	Global
Kinds of model:	Physics-based models	Statistical models

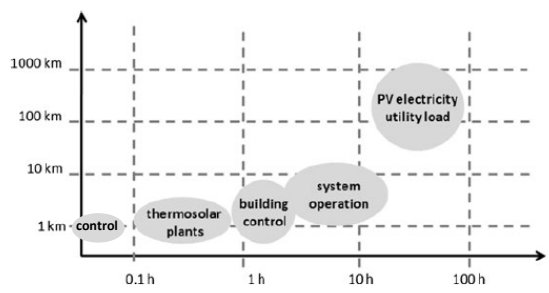




Fig. 2.2 Spatial and temporal scales of target applications, [175]


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## Ingredients: Solar energy is a disturbance and the main source of energy

Short-term forecast (15 minutes) useful for predictive control

A. Pawlowski, J.L. Guzmán, M. Berenguel, F. Rodríguez, J. Sánchez. Application of time-series methods to disturbance estimation in predictive control problems. **International Symposium on Industrial Electronics ISIE'10**, 409-414, Bari, Italy, 2010.

- A. Discrete Kalman Filter
- B. Discrete Kalman Filter with Data Fusion
- C. Exponentially Weighted Moving Average
- D. Double Exponential Smoothing**

$z_k$  measurement

$S_k$  unadjusted forecast

$b_k$  estimated trend

$$S_k = \alpha z_k + (1 - \alpha)(S_{k-1} + b_{k-1})$$

$$b_k = \gamma(S_k - S_{k-1}) + (1 - \gamma)b_{k-1}$$

can be obtained via optimization techniques

$\alpha$  smoothing parameter for data (0,1)

$\gamma$  smoothing parameter for trend (0,1)

The one-period-ahead forecast is given by:

$$\hat{x}_{k+1} = S_k + b_k$$


The  $m$ -periods-ahead forecast is given by:


$$\hat{x}_{k+m} = S_k + mb_k$$

NIST. (2006) Engineering statistics handbook. [Online]. Available: <http://www.itl.nist.gov/div898/handbook/index.htm>


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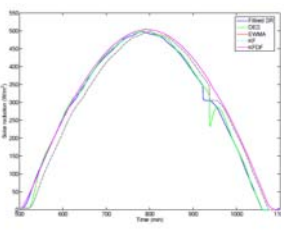
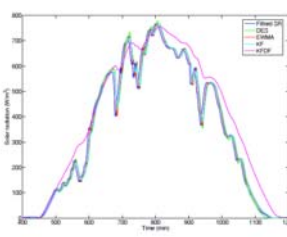
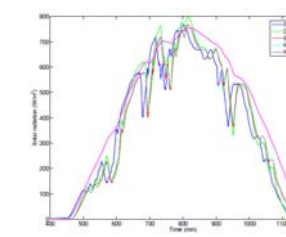


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Ingredients: Solar energy is a disturbance and the main source of energy

Short-term forecast (15 minutes) useful for predictive control







Results for a clear day with a 15-samples horizon
Results for a day with passing clouds and a 5-samples horizon
Results for a day with passing clouds and a 15-samples horizon

Alternative: "lazy man" weather approach


The same approach can be used for other disturbances (temperature, wind, ...)

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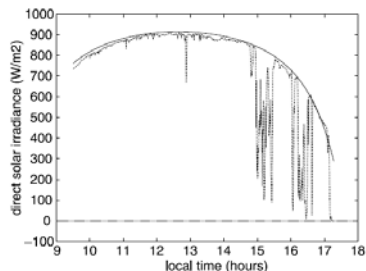
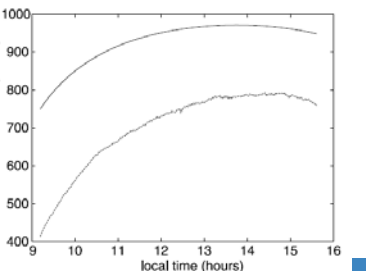
Ingredients: Solar energy is a disturbance and the main source of energy

Clear day prediction

Extraterrestrial Radiation on Horizontal Surface:  $I_{ho}(h, J) = I_{SC} \epsilon_o \cos \theta_{ZS}$

where  $I_{ho}$  is the instant solar radiation,  $h$  is the local time,  $J$  is the day number in Julian calendar,  $I_{SC}$  is the solar constant,  $\epsilon_o$  is the distance between sun and earth, and  $\theta_{ZS}$  is the sun zenithal distance.


Similar models for direct beam irradiance





(a) November 26th, 1990
(b) September 19th, 1991


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11



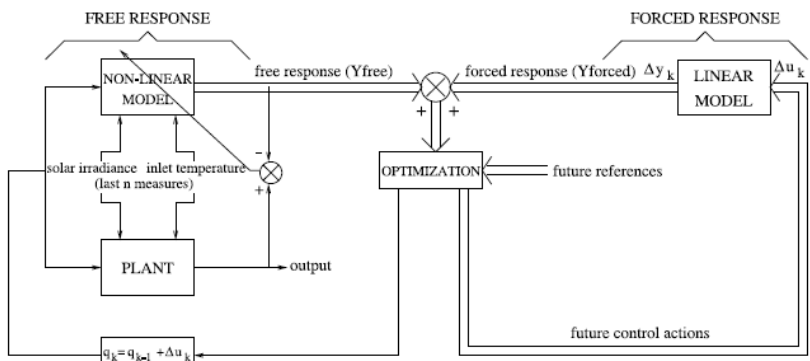


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### Ingredients: Solar energy is a disturbance and the main source of energy


Clear day prediction




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12







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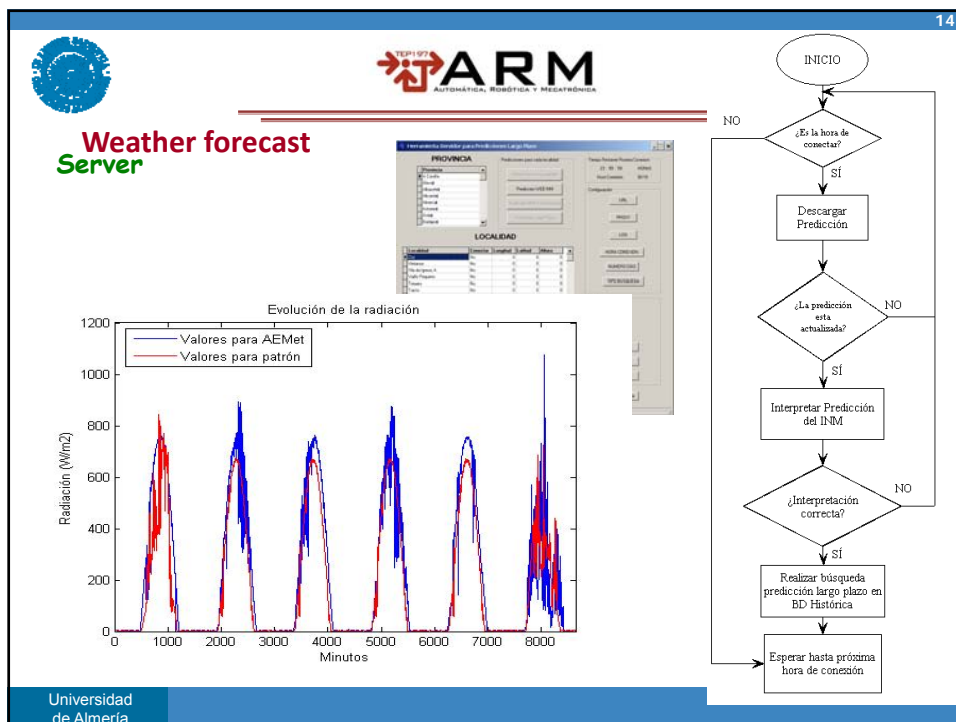
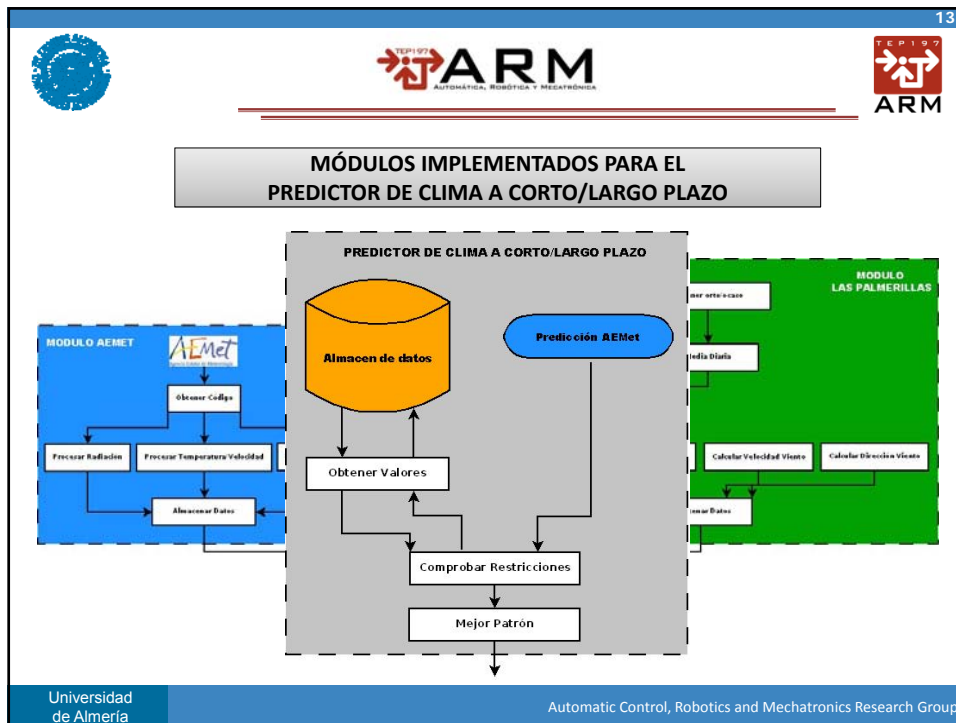


### Ingredients: Solar energy is a disturbance and the main source of energy


Long-term prediction


Ejido, El (80 m) - ALMERÍA		Elaborado: 01.09.2004 07:50 (hora local peninsular)									
Fecha	Miércoles 01		Jueves 02		Viernes 03		Sáb 04	Dom 05	Lun 06	Mar 07	
	a.m.	p.m.	a.m.	p.m.	a.m.	p.m.					
Estado del cielo											
Probabilidad de precipitación (%)	0		10		20		25	15	20	15	
T. Máxima (°C)	32		30		29		31	32	31	31	
T. Mínima (°C)	19		19		19		20	21	20	20	
Viento (Km/h)	Calma 7		11 11		7		Calma	11	7	7	
Índice UV Máximo	7		8		8						



15



# Index




**Motivation and main objectives**

- The CIESOL building
- Comfort in buildings
  - Predicted Mean Vote (PMV) index
  - PMV index approximations
- Thermal comfort control inside a room
  - Linear Predictive Control
  - First principles model of a room
  - A Practical Non-Linear Model Predictive Control (PNMPC) approach
- Actual works


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16



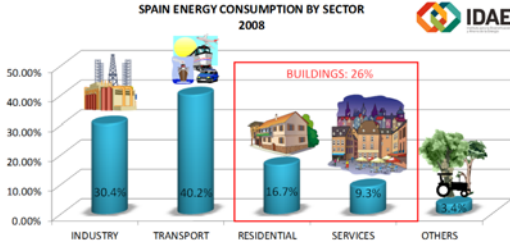
# Motivation



- Energy consumption in buildings represents about 40% of total world energy consumption, more than half used by HVAC (Heating, Ventilation and Air Conditioning) Systems. Moreover, they are also responsible of approximately 35% of CO<sub>2</sub> emissions.



**SPAIN ENERGY CONSUMPTION BY SECTOR 2008**



Sector	Percentage
INDUSTRY	30.4%
TRANSPORT	40.2%
BUILDINGS (Residential + Services)	26%
RESIDENTIAL	16.7%
SERVICES	19.3%
OTHERS	0.00%


- **MAIN OBJECTIVE**  
- To provide comfortable environments with the minimum possible energy consumption.

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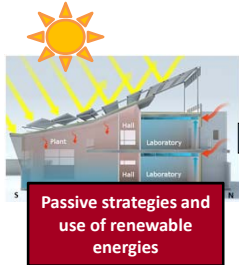
17



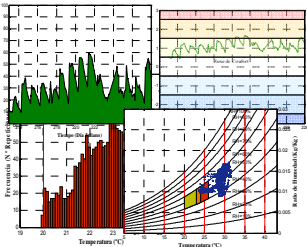
## Main objectives

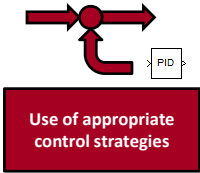


1. To study and analyze users' comfort inside a building from both thermal comfort and indoor air quality points of view.
2. Development of a methodology for design, calibration and validation of physical models with unknown parameters.
3. Study, analysis and development of advanced control techniques for the comfort control problem.
4. Test and integration in a control architecture of the developed strategies in order to analyze its behaviour.



Passive strategies and use of renewable energies






Use of appropriate control strategies


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## Scope of the research



**PSE-ARFRISOL research project**  
(M. Rosario Heras – CIEMAT)



- It is a singular strategic project about bioclimatic architecture and solar cooling.





**POWER+ENERPRO research projects**  
(Francisco Rodríguez+Manuel Berenguel)

- Supervision and control strategies for the integrated management of installations inside energy efficient environments.








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19




# Index




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    - Predicted Mean Vote (PMV) index
    - PMV index approximations
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# CIESOL building




**Passive strategies**




- Solar collectors field:** To produce hot water for the solar cooling installation and for the shading of the plant roof
- Photovoltaic panels:** To produce energy and for the shading of the laboratories which faces north
- Enclosure north and plant facade:** 20cm thickness thermo-clay block, 3cm thickness sprayed polyurethane foam insulation, and a covering of galvanized steel wavy sheet
- Ventilated facade:** quoted perforated brick, a 3cm thickness sprayed polyurethane foam insulation, a wall cavity, and a compact ceramic tiling
- Plant with inclined roof:** crossed ventilation
- Setback of the windows:** to avoid direct influence of solar radiation in hot months
- Glazed enclosure:** a climatic double thermo-acoustic piece of glass


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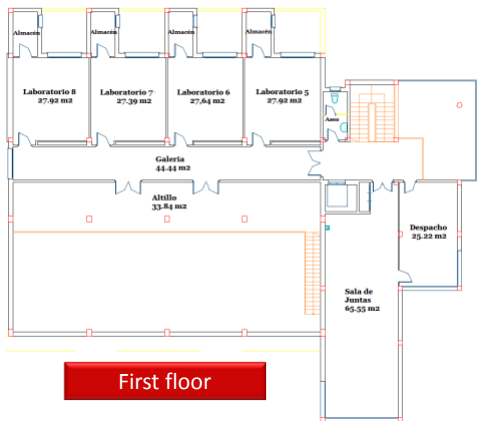


# CIESOL building





**Ground floor**




**First floor**


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# CIESOL building

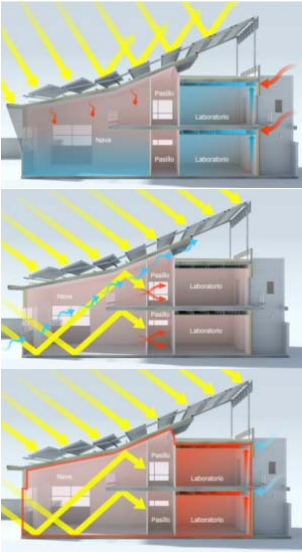


*Passive strategies*

Closing composed by waved sheet, isolation and thermo-clay blocks

Ventilated façade with external ceramic facing, air chamber, polyurethane isolation and high thermal inertia wall





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# CIESOL building




Active strategies: Solar cooling installation

- This research centre was built following a bioclimatic architecture criteria, where HVAC systems are based on solar cooling using a solar collectors field, a hot water storage system, a boiler, and an absorption machine with its refrigeration tower.





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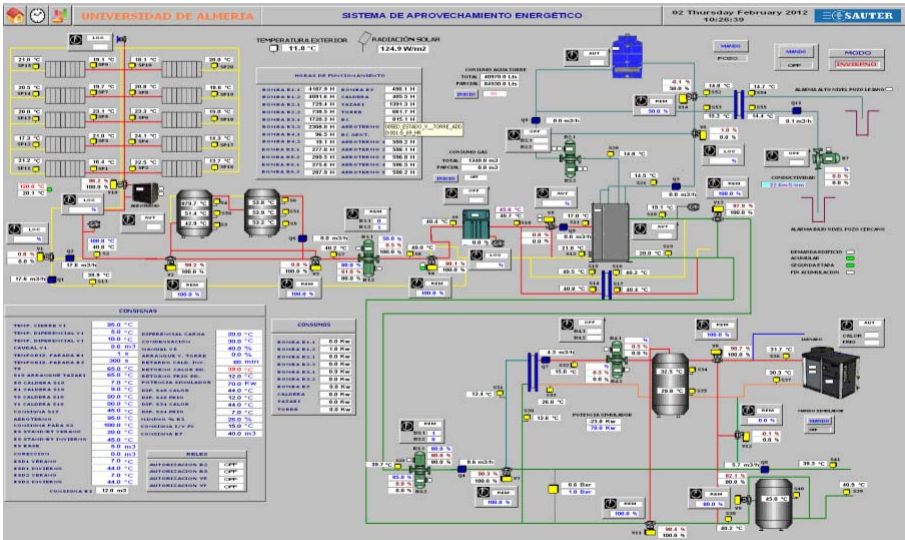
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# CIESOL building



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# CIESOL building



Other active strategies









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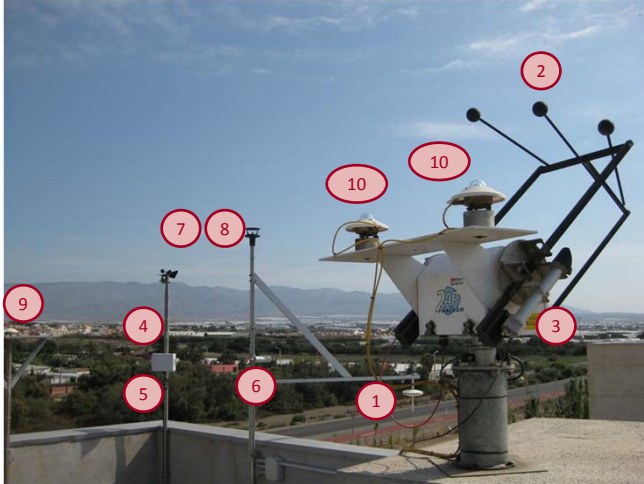


# CIESOL building



Sensors network of the building: Meteorological station


1. Atmospheric pressure
2. Solar tracking
3. Pyrheliometer
4. Air temperature
5. Relative humidity
6. CO2 concentration
7. Wind velocity
8. Wind direction
9. Pygeometer (infrared radiation)
10. Pyranometer (direct and diffuse irradiances)




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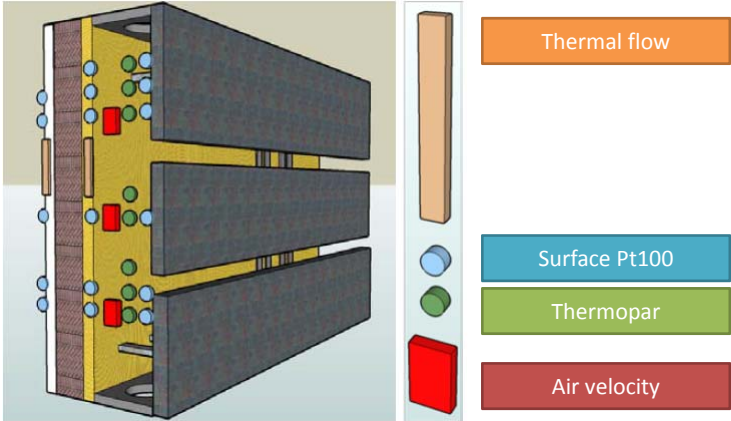
27



## CIESOL building



*Sensors network of the building: Ventilated façade*



- Thermal flow
- Surface Pt100
- Thermopar
- Air velocity

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28



## CIESOL building



*Sensors network of the building: Representative rooms of the building*



Room 110



Laboratory 6



Room 070



Meeting room



Laboratory 8

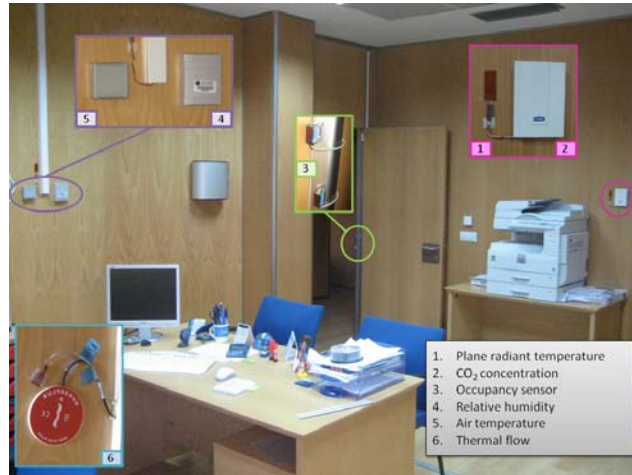
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# CIESOL building



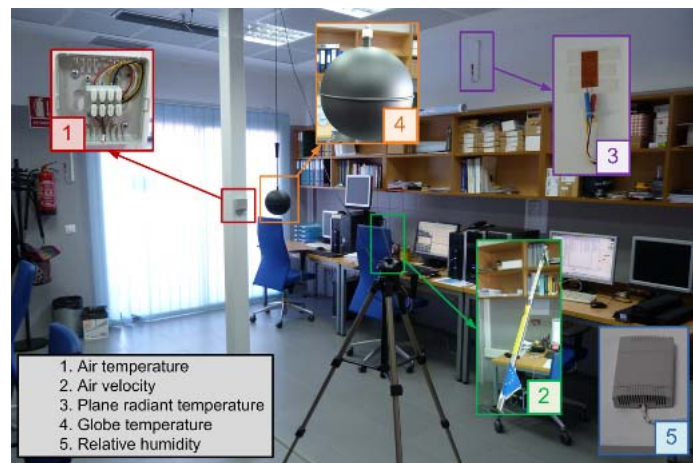
Sensors network. A characteristic room of the building




# CIESOL building




Sensors network of the building: Representative rooms of the building



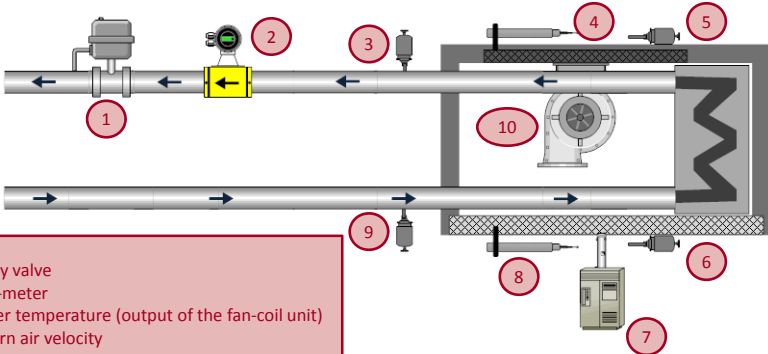
31



## CIESOL building



*Sensors network of the building: fan-coil units*




1. 2-Way valve
2. Flow-meter
3. Water temperature (output of the fan-coil unit)
4. Return air velocity
5. Return air temperature
6. Impulse air temperature
7. Impulse relative humidity
8. Impulse air velocity
9. Water temperature (input of the fan-coil unit)
10. Fan (0 - 33 - 66 - 100%)


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## CIESOL building



*Sensors network of the building: Room occupation system*








Also with Xbox Kinect

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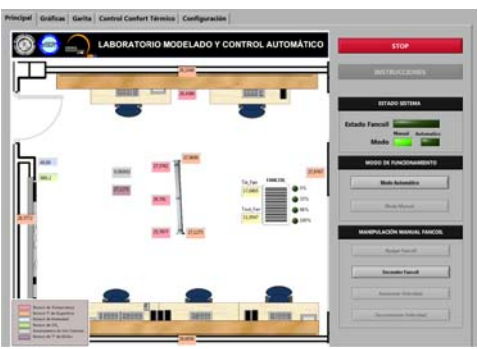


33



## CIESOL building





*Monitoring and acquisition applications:  
around 400 sensors and actuators  
integrated via OPC using a dedicated  
Ethernet network*

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34



## Index




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    - Predicted Mean Vote (PMV) index
    - PMV index approximations
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## Thermal comfort




Thermal Comfort?

ISO 7730


ASHRAE 55





"That condition of mind which expresses satisfaction with the thermal environment"

Condition  
of mind



Satisfaction

"Comfort is a cognitive process which depends of different kinds of processes, such as, physical, physiological or even psychological"

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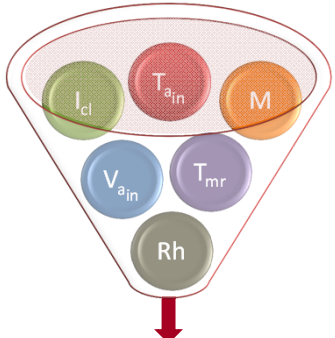
36

## Thermal comfort

**Predicted Mean Vote (PMV) Index**

- This index is able to predict the average response about thermal sensation of a large group of people exposed to certain thermal conditions for a long time.


+3	Hot
+2	Warm
+1	Slightly warm
0	Neutral
-1	Slightly cool
-2	Cool
-3	Cold




PMV Index

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# Thermal comfort



**Predicted Mean Vote (PMV) Index**

**Classical approach**

- The PMV index can be estimated as a function of the six previous variables just as:

$$PMV = [0.303 \exp(-0.036M) + 0.028]L$$

where


*M*: Metabolic rate  
*L*: Thermal load in the human body

$$L = (M - W) - 0.0014 \cdot M \cdot (34 - T_{a,in}) - 3.05 \cdot 10^{-3} \cdot [5733 - 6.99 \cdot (M - W) - p_{a,in}] - 0.42 \cdot (M - W - 58.15) - 1.72 \cdot 10^{-5} \cdot M \cdot (5867 - p_{a,in}) - 39.6 \cdot 10^{-9} \cdot F_{cl} \cdot [(T_{cl} + 273)^4 - (T_{mr} + 273)^4] - F_{cl} \cdot h_c \cdot (T_{cl} - T_{a,in})$$


Acronym	Meaning
<i>W</i>	Effective mechanical power
$T_{a,in}$	Air temperature
$p_{a,in}$	Partial water vapor pressure in the air
$F_{cl}$	Clothing area factor
$T_{cl}$	Clothing surface temperature
$T_{mr}$	Mean radian temperature
$h_c$	Convective heat transfer coefficient

Función no lineal de otras variables (si no se miden) o valores tabulados

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# Thermal comfort

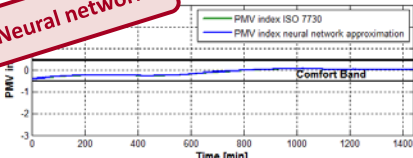


**Predicted Mean Vote (PMV) Index**

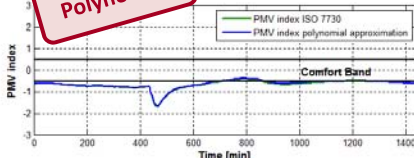
**PMV index approximations**

- To reduce computational costs and price of sensors network in order to estimate PMV index different black box models based on neural networks and polynomial approximations has been obtained.

**Neural networks**




**Polynomial**




Model	RMSE			
	VA1a	VA1b	VA2a	VA2b
ANN	0.0117	0.0079	0.0145	0.0123
Polynomial	0.0065	0.0357	0.0296	0.0528

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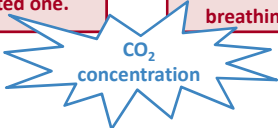
## Air quality



**prEN 15251**      **Air Quality?**      **prEN 13779**

To perceive fresh air, instead of vitiated, loaded or irritated one.

To know that the risk for the health which could be derived from breathing that air is depreciable




CO<sub>2</sub> concentration

- In accordance with international standards, just as prEN 13779 and prEN 15251, indoor air quality could be classified by CO<sub>2</sub> concentration since it is the main bioeffluent from human respiratory


Category	Description	Typical range	Default value
IDA 1	High indoor air quality	≤400	350
IDA 2	Medium indoor air quality	400 – 600	500
IDA 3	Moderate indoor air quality	600 – 1000	800
IDA 4	Low indoor air quality	> 1000	1200

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## Air quality



**Indoor Air Quality (IAQ) Index**


- This index allows to classify indoor air for occupied rooms, where smoking is not allowed and pollution is caused mainly by human metabolism, according to the four indoor air quality categories.

$$IAQ = 0.001 \cdot CO_{2m} - 0.5$$


IAQ ≤ 0	High indoor air quality (IDA 1)
0 < IAQ < 0.1	Medium indoor air quality (IDA 2)
0.1 ≤ IAQ < 0.5	Moderate indoor air quality (IDA 3)
0.5 ≤ IAQ ≤ 1	Low indoor air quality (IDA 4)

- To guarantee indoor air quality in a certain environment, it is recommended to maintain a CO<sub>2</sub> concentration level between 500 ppm and 600 ppm, that is an IAQ index value at 0 with a tolerance of 0.1.

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# Comfort analysis




- The main objective of this study is to evaluate the performance of the passive bioclimatic strategies of the CDDI-CIESOL-ARFRISOL building without the use of any control strategy.
- As the building does not have a fixed work schedule, the following assumptions has been established:
  - Saturdays and Sundays are considered periods of non occupation, that is, the building is supposed to be empty.
  - Within the occupation periods (from Monday to Friday) it is established a night time period that comprise from 21:00 PM to 07:00 AM.


Almería characteristic climate	Summer	Winter	Autumn
Maximum mean air temperature [°C]	30.7	17.7	20.4
Minimum mean air temperature [°C]	22	8.8	12.0
Mean relative humidity [%]	65	68	70
Average precipitation days [-]	0	3	3
Mean monthly sunshine hours [-]	312	191	187

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# Comfort analysis



**Thermal comfort analysis. Summer period**  
**From 1<sup>st</sup> (Saturday) to 15<sup>th</sup> (Saturday) of August 2009.**

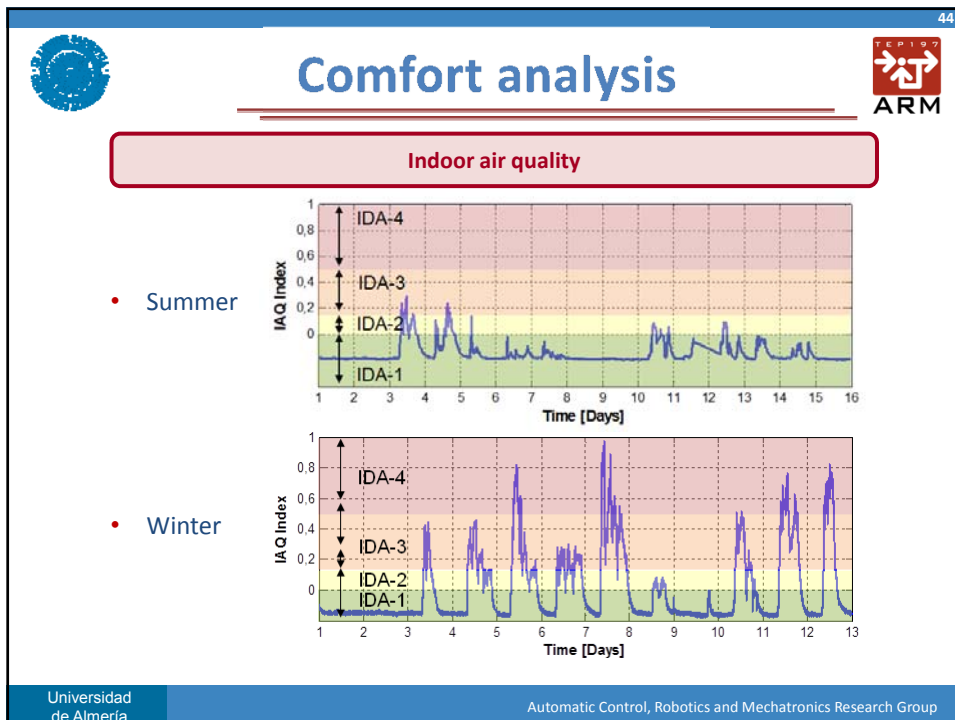
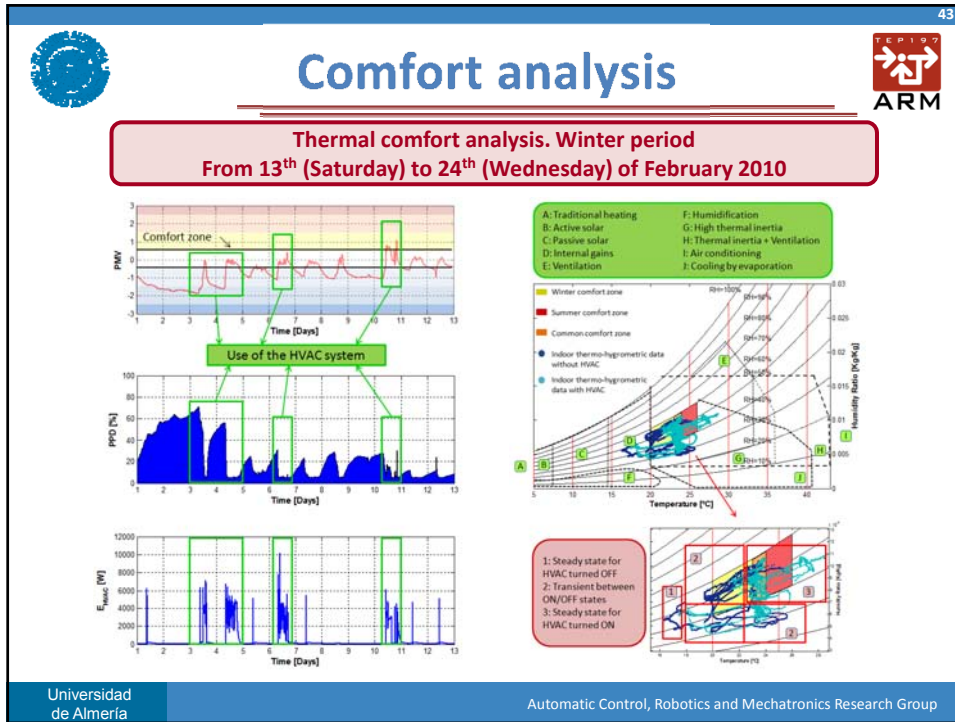
A: Traditional heating  
 B: Active solar  
 C: Passive solar  
 D: Internal gains  
 E: Ventilation

F: Humidification  
 G: High thermal inertia  
 H: Thermal inertia + Ventilation  
 I: Air conditioning  
 J: Cooling by evaporation


1: Stationary state for HVAC turned OFF  
 2: Transient state between ON and OFF states  
 3: Stationary state for HVAC turned ON

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45



## Comfort analysis




**Main conclusions of the comfort analysis**


- For both summer and winter periods, it is necessary the use of a HVAC system to cool in summer, and to heat in winter.
- The existence of a significant percentage of data outside the comfort zone during summer and winter periods allows to consider two hypothesis which are not strictly exclusive:
  - Insufficiency of manual control that was implemented in the HVAC system.
  - Existence of subjective factors in the evaluation of both thermal comfort and indoor air quality.
- As a function of this comfort analysis, it has reached the conclusion that it was necessary to develop a specific control system which allows to maintain environmental conditions of the building inside a comfort zone for the user minimising, at the same time, energy consumption.

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46




## Index




- Motivation and main objectives
- The CIESOL building
- Comfort in buildings
  - Predicted Mean Vote (PMV) index
  - PMV index approximations
- **Thermal comfort control inside a room**
  - Linear Predictive Control
  - First principles model of a room
  - A Practical Non-Linear Model Predictive Control (PNMPC) approach
- Actual works

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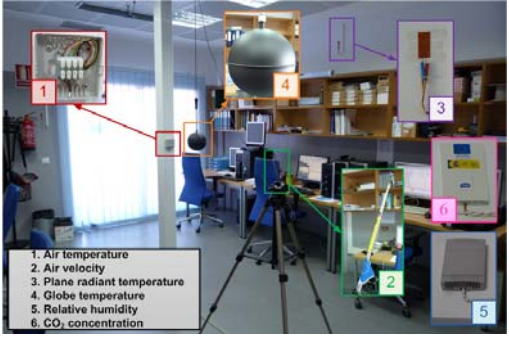
## Indoor climate model of a room



Models allow to obtain important information about systems, and thus, they represent a key factor in order to design control strategies and solve optimization problems.

**A typical CDDI-CIESOL-ARFRISOL office room**


- Room location: second floor of the building.
- Total volume:  $4.96 \times 5.53 \times 2.8 \text{ m}^3$
- North orientation
- Number of windows: 1
- Window surface:  $2.15 \times 2.09 \text{ m}^2$
- Window location: north wall
- Actuators:
  - Window opening/closing system
  - Shading opening/closing system
  - HVAC fan power
  - HVAC water flow valve




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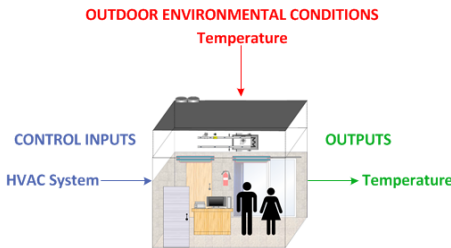
## Indoor climate model of a room



**A Linear Time-Invariant (LTI) temperature model**

**Assumptions:**

- The state variable of the system is the indoor air temperature.
- There exist only one element which interact with the indoor air temperature: the external air.
- As control variable, it was supposed that there was only one actuator available, the fancoil unit, which allows to control indoor air temperature by means of its fan velocity.
- It is considered that all the variables of the process are homogenously distributed.




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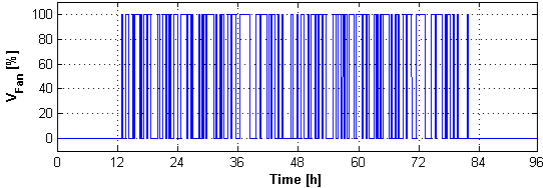


## Indoor climate model of a room



**A Linear Time-Invariant (LTI) temperature model**

- PRBS Signal: Pseudo – Random Binary Signal




- ARX Model: AutoRegressive model with eXogeneous input

$$y(t) + a_1 y(t-1) + \dots + a_{na} y(t-na) = b_1 u(t-nk) + \dots + b_{nb} u(t-nk-nb+1)$$


where  $na$  is the number of poles,  $nb+1$  is the number of zeros and  $nk$  is the delay of the system if it exists.

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50

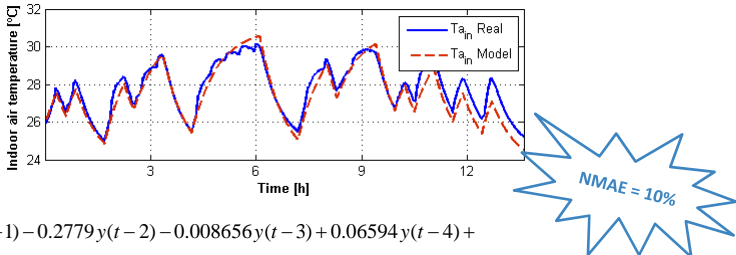


## Indoor climate model of a room



**A Linear Time-Invariant (LTI) temperature model**

- Cross validation results for the LTI indoor temperature model




$$y(t) - 0.9417y(t-1) - 0.2779y(t-2) - 0.008656y(t-3) + 0.06594y(t-4) + 0.1009y(t-5) + 0.06291y(t-6) = 0.0001126u(t)$$


At present, grey-box models considering simplified balances (R,C circuits) so that only a few parameters have to be identified.

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51



## Indoor climate model of a room

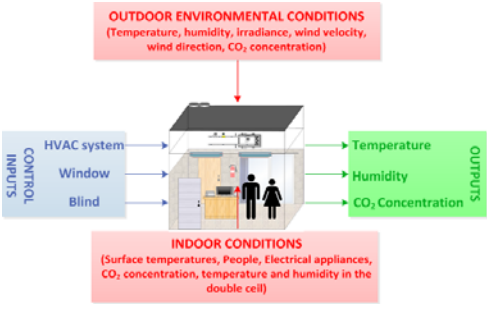


**A first principles model of a room**

- The first principles model of a room is composed of three submodels which describe the indoor air temperature, the indoor air relative humidity and the indoor CO<sub>2</sub> concentration dynamic behaviour. Hence, it can be represented by a system of differential equations given by:

$$\frac{dX}{dt} = f(X, U, D, V, C, t) \text{ with } X(t_i) = X_i$$

where  $X$ ,  $U$ ,  $D$ ,  $V$  and  $C$  are vectors of the state variables, control inputs variables, disturbances, system variables and system constants, respectively,  $t$  is the time,  $X_i$  is the known initial state at the initial time  $t_i$ , and  $f$  is a nonlinear function based on mass and heat transfer balances.




The diagram illustrates a room model with the following components:

- OUTDOOR ENVIRONMENTAL CONDITIONS** (Temperature, humidity, irradiance, wind velocity, wind direction, CO<sub>2</sub> concentration) - Input from the top.
- CONTROL INPUTS** (HVAC system, Window, Blind) - Inputs from the left.
- INDOOR CONDITIONS** (Surface temperatures, People, Electrical appliances, CO<sub>2</sub> concentration, temperature and humidity in the double cell) - Internal state of the room.
- OUTPUTS** (Temperature, Humidity, CO<sub>2</sub> Concentration) - Outputs from the right.


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## Indoor climate model of a room



**A first principles model of a room**


**Assumptions:**

- It is supposed that the room is composed by seven elements: indoor air, walls, windows, shading system, HVAC system, people and electrical appliances.
- The state variables of the model are: indoor air temperature, indoor relative humidity and CO<sub>2</sub> concentration.
- The control inputs of the system are: the natural ventilation, expressed as a function of the window opening, the blind, and the forced ventilation by means of a fancoil unit.
- The disturbance inputs of the system are: the outside air temperature, humidity and CO<sub>2</sub> concentration, wind speed and its direction, direct, diffuse and reflected irradiance, the plane radiant temperatures of all surfaces of the room, indoor air velocity, number of people inside the room and the electrical appliances that are connected at each moment.
- The physical characteristics of the different elements (walls, windows, etc.) such as density or specific heat are considered constant. However, the physical characteristics of the air inside the room are estimated as a function of indoor air temperature.


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## Indoor climate model of a room



**A first principles model of a room**

Temperature model

Humidity model

CO<sub>2</sub> concentration model


$$m_a \cdot C_{p_a} \cdot \frac{dT_{a_m}}{dt} = \underbrace{Q_{conv}}_{\text{Convection}} + \underbrace{Q_{glass}}_{\text{Window}} + \underbrace{Q_{fv}}_{\text{Forced Ventilation}} + \underbrace{Q_{nvt}}_{\text{Natural ventilation}} + \underbrace{Q_{inf}}_{\text{Infiltrations}} + \underbrace{Q_{tGain}}_{\text{Internal gains}}$$

$$V_{a_m} \rho_{a_m} \frac{dW_{a_m}}{dt} = \underbrace{M_{w_p}}_{\text{People}} + \underbrace{M_{w_f}}_{\text{Forced ventilation}} + \underbrace{M_{w_{inf}}}_{\text{Infiltrations}} + \underbrace{M_{w_{nvt}}}_{\text{Natural ventilation}}$$


$$V_{a_m} \frac{dCO_{2_m}}{dt} = \underbrace{MCO_{2_p}}_{\text{People}} + \underbrace{MCO_{2_{nvt}}}_{\text{Natural ventilation}} + \underbrace{MCO_{2_f}}_{\text{Forced ventilation}} + \underbrace{MCO_{2_{inf}}}_{\text{Infiltrations}}$$

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54



## Indoor climate model of a room



**A first principles model of a room**


**Calibration and Validation methodology**

**Main problem: an important set of unknown parameters**


- Data of the climate variables to model, the disturbances and the actuators state are measured and stored in a database, thus, the main parameters estimation and the calibration problem can be divided into three submodels calibration processes.
- Some of the processes which are involved in each one of the balance equations do not have any influence in determined periods of a day or they are not coupled. Thus, all the parameters of a single submodel do not have to be estimated simultaneously.
- Some processes have to be modelled in different forms based on determined situations.
- Some controlled experiments tests can be performed into the room in order to estimate the parameters associated with the actuators.

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55



## Indoor climate model of a room



**A first principles model of a room**

Calibration and Validation methodology


- The proposed methodology consists of a two steps calibration process:
  - First step. To determine a search space by means of an iterative search by performing single experimental tests for each one of the involved processes.
  - Second step. To obtain the final value for each one of the unknown parameters by means of genetic algorithms.

$$\begin{aligned}
 J(x) &= \min \sum_{i=1}^N |x(i) - \hat{x}(i, \Psi)|^2 = \\
 &= \min \sum_{i=1}^N \sum_{k=1}^3 |x_k(i) - \hat{x}_k(i, \Psi)|^2
 \end{aligned}$$


where  $N$  is the number of samples and  $k$  is the number of models which are going to be calibrated.

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56



## Indoor climate model of a room

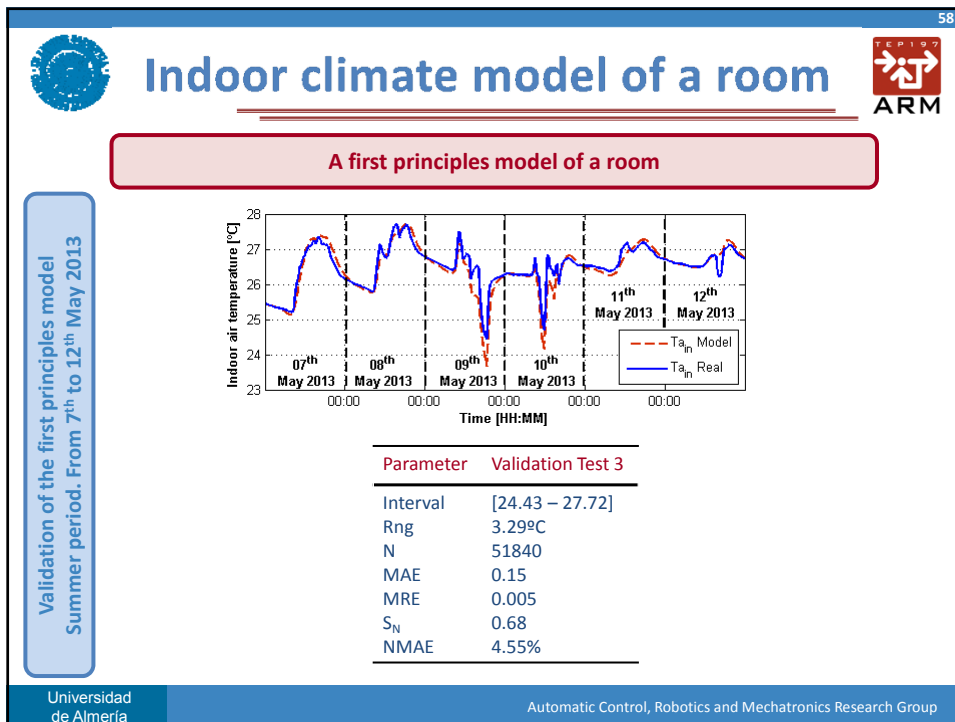
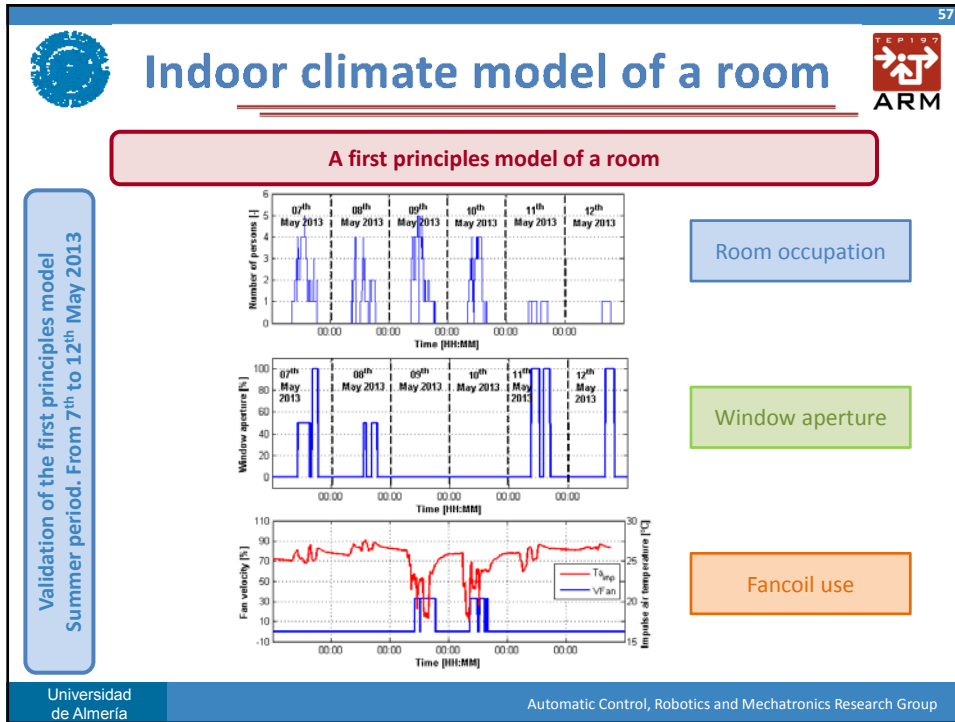


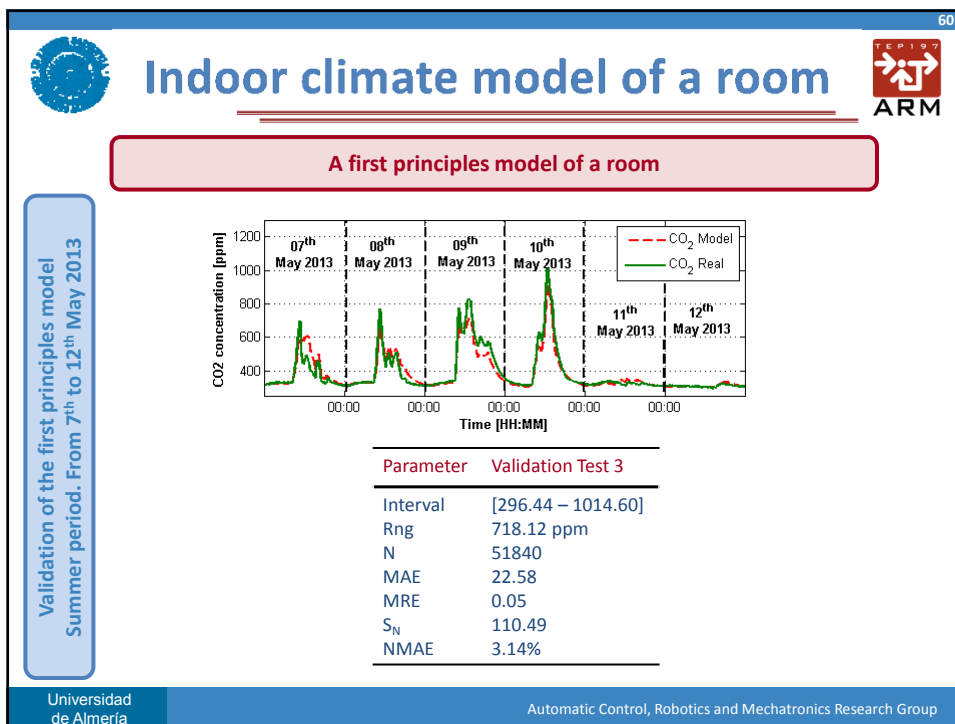
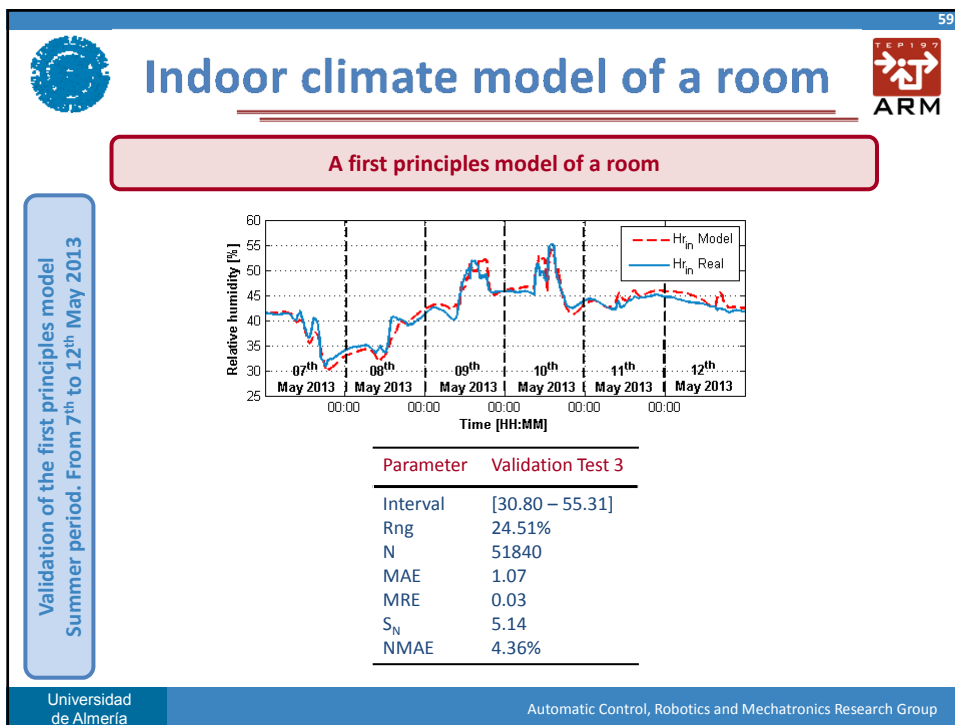
**A first principles model of a room**

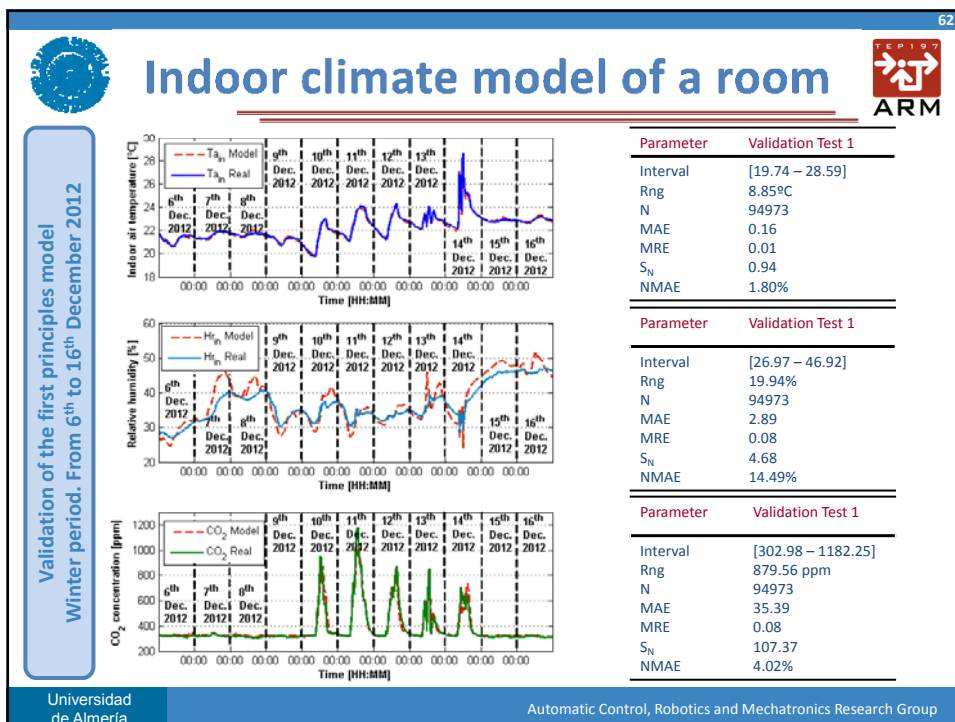
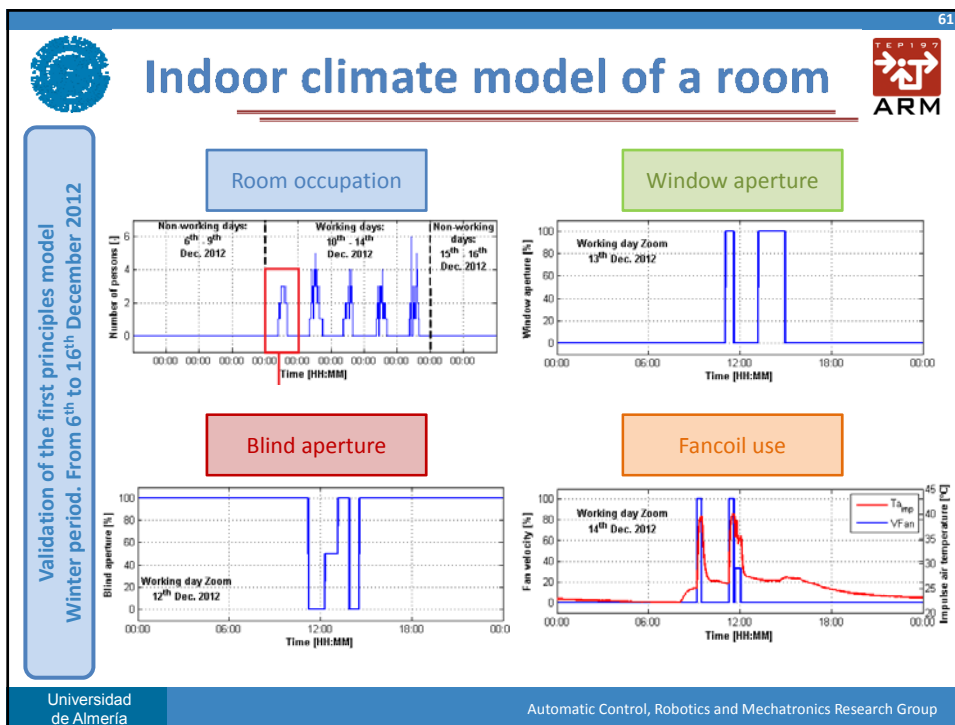
Calibration and Validation methodology


- Test 1. Empty room and blind closed (5).
- Test 2. Empty room and blind open (1).
- Test 3. Empty room and blind in several positions (6).
- Test 4. Empty room and using forced ventilation (1).
- Test 5. Empty room and using natural ventilation (1).
- Test 6. Occupied room (1).
- Test 7. Occupied room and using natural ventilation (2).
- Test 8. Validation of the selected unknown parameters (10).

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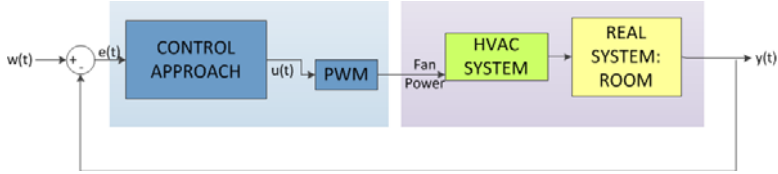


## Linear controllers for users' thermal comfort




63

- **Main objective.** To obtain a high thermal comfort level taking energy costs into account.
- To do that, it has been considered that there is only one actuator available inside the CDDI-CIESOL-ARFRISOL building in order to control thermal comfort, the HVAC system.
- Two different approaches are presented:
  - A hierarchical predictive control strategy.
  - A classical Model Predictive Control (MPC) strategy.




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## Thermal comfort control inside a room



64

**Generalized Predictive Control Algorithm**

Controller Auto-Regressive Integrated Moving-Average (CARIMA)

$$A(z^{-1})y(t) = z^{-d}B(z^{-1})u(t-1) + C(z^{-1})\frac{e(t)}{\Delta}$$

$$\Delta = 1 - z^{-1}$$

$A(z^{-1}) = 1 + a_1z^{-1} + a_2z^{-2} + \dots + a_naz^{-na}$ 
 $B(z^{-1}) = b_0 + b_1z^{-1} + b_2z^{-2} + \dots + b_nbz^{-nb}$ 
 $C(z^{-1}) = 1 + c_1z^{-1} + c_2z^{-2} + \dots + c_ncz^{-nc}$

Quadratic Cost Function

$$J = \sum_{j=N_1}^{N_2} \delta(j)[\hat{y}(t+j|t) - w(t+j)]^2 + \sum_{j=1}^{N_u} \lambda(j)[\Delta u(t+j-1)]^2$$


- D.W. Clarke, C. Mohtadi and P.S. Tufts. *Generalized predictive control I. The basic algorithm*. Automatica, 23, 137-148, 1987
- E.F. Camacho, C. Bordóns. *Model Predictive Control*. Springer, 2012.
- One of the most popular MPC algorithm in both industry and academy.

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65



## Thermal comfort control inside a room



**Generalized Predictive Control Algorithm**

Obtaining the GPC Control Law

- The predicted outputs,  $\hat{y}(t+k|t)$ , are calculated using the prediction model ( $C(z^{-1})=1$ ):

$$A(z^{-1})y(t) = z^{-d}B(z^{-1})u(t-1) + C(z^{-1})\frac{e(t)}{\Delta} \quad \Rightarrow \quad y = \underbrace{Gu}_{\text{forced response}} + \underbrace{f}_{\text{free response}}$$

- Substitute the compact prediction values in the cost function,  $J$ .


$$J = \sum_{j=N_1}^{N_2} \delta(j)[\hat{y}(t+j|t) - w(t+j)]^2 + \sum_{j=1}^{N_u} \lambda(j)[\Delta u(t+j-1)]^2 \quad \Rightarrow \quad J = (Gu + f - w)^T(Gu + f - w) + \lambda u^T u$$

- Minimize  $J$  with respect to  $\Delta u$  where an analytical solution is obtained for the unconstrained case:


$$u = -H^{-1}b = (G^T G + \lambda I)^{-1} G^T (w - f) \quad \Rightarrow \quad u(t) = u(t-1) + K(w - f)$$

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66



## Thermal comfort control inside a room



**Generalized Predictive Control Algorithm**

Obtaining the GPC Control Law (future predictions):

$$y = \underbrace{Gu}_{\text{forced response}} + \underbrace{f}_{\text{free response}}$$


The prediction outputs,  $y(t+j)$ , must be obtained for  $j \geq N_1$  and  $j \leq N_2$ . The horizons can be set as  $N_1=d+1$ ,  $N_2=d+N$ ,  $N_u=N$ . Thus,  $N$ -ahead predictions will be used in the optimization process.

The predictions could be done just from the CARIMA model:


$$\begin{aligned} \hat{y}(t+d+j|t) &= (1 - a_1)\hat{y}(t+d+j-1|t) + \\ &+ (a_1 - a_2)\hat{y}(t+d+j-2|t) + \dots + a_{na}\hat{y}(t+d+j-n_a-1|t) + \\ &+ b_0\Delta u(t+j-1) + \dots + b_{nb}\Delta u(t+j-n_b-1) \end{aligned}$$

This is really done using a Diophantine Equation.

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## Thermal comfort control inside a room



**Generalized Predictive Control Algorithm**

Dealing with constraints:  
 Typical Quadratic Programming (QP) Problem:

$$J = \frac{1}{2} \mathbf{u}^T \mathbf{H} \mathbf{u} + \mathbf{b}^T \mathbf{u} + \mathbf{f}_0 \qquad J = \frac{1}{2} \mathbf{x}^T \mathbf{H} \mathbf{x} + \mathbf{f}^T \mathbf{x}$$

$$\mathbf{R} \mathbf{u} \leq \mathbf{c} \qquad \mathbf{R} \mathbf{x} \leq \mathbf{c}$$


$$\mathbf{E} \mathbf{u} = \mathbf{g} \qquad \mathbf{E} \mathbf{x} = \mathbf{g}$$

Minimization of a quadratic function with linear constraints. Example:  
**quadprog** function of *Matlab*.


QUADPROG Quadratic programming.  
 X = QUADPROG(H,f,A,b) attempts to solve the quadratic programming problem:

```


min 0.5*x'*H*x + f'*x  subject to:  A*x <= b
x
  
```



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## Thermal comfort control inside a room



**Generalized Predictive Control Algorithm**


Dealing with constraints:  
 Different types of constraints:

- **Physical or security constraints:** process limitations.
- **User-defined constraints:** to force derided output.
- **Input:** typical saturation constraints.
- **Output:** operation conditions.


All of them must be defined based on control increments  $\Delta u$  ( $\mathbf{u}$ ).

$$\mathbf{R} \mathbf{u} \leq \mathbf{c}$$


$$\mathbf{E} \mathbf{u} = \mathbf{g}$$



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## Thermal comfort control inside a room




**Generalized Predictive Control Algorithm**


Dealing with constraints:

Variable	Linear constraint
Control signal amplitude (U) $u_{\min} \leq u(t) \leq u_{\max}$	$\Gamma u_{\min} \leq \Upsilon \Delta u + u(t-1) \Gamma \leq \Gamma u_{\max}$
Control signal increment (DU) $\Delta u_{\min} \leq u(t) - u(t-1) \leq \Delta u_{\max}$	$\Gamma \Delta u_{\min} \leq \Delta u \leq \Gamma \Delta u_{\max}$
Output signal amplitude (Y) $y_{\min} \leq y(t) \leq y_{\max}$	$\Gamma y_{\min} \leq G \Delta u + f \leq \Gamma y_{\max}$
Envelope constraints (Y Band) $y_{\min}(t) \leq y(t) \leq y_{\max}(t)$	$G \Delta u \leq y_{\max} - f; y_{\max} = [y_{\max}(t+1) \dots y_{\max}(t+N)]$ $G \Delta u \leq y_{\min} - f; y_{\min} = [y_{\min}(t+1) \dots y_{\min}(t+N)]$
Output overshoot $y(t+j) \leq y_w(t); j = N_{o1} \dots N_{o2}$	$G \Delta u \leq \Gamma y_w(t) - f$
Output monotone behavior $y(t+j) \leq y(t+j+1)$ if $y(t) < w(t)$ $y(t+j) \geq y(t+j+1)$ if $y(t) > w(t)$	$G \Delta u + f \leq [(0^T/G') \Delta u + [(y(t)/f')]^T]$ $G'$ and $f'$ are the result of eliminating the last row of $G$ and $f$ .
Limit inverse response (NMP) $y(t+j) \leq y(t)$ if $y(t) > w(t)$ $y(t+j) \geq y(t)$ if $y(t) < w(t)$	$G \Delta u \geq \Gamma y(t) - f$
Final state $y(t+N+1) \dots y(t+N+m) = w$	$y_m = [y(t+N+1) \dots y(t+N+m)]^T$ $y_m = G_m \Delta u + f_m; \quad G_m \Delta u = w_m - f_m$
Output integral $T_m \sum_{t=1}^{t+N} y(t) = I$	$\Gamma^T \begin{bmatrix} y(t+1) \\ \vdots \\ y(t+N_j) \end{bmatrix} = G_i \Delta u + f_i \geq I$

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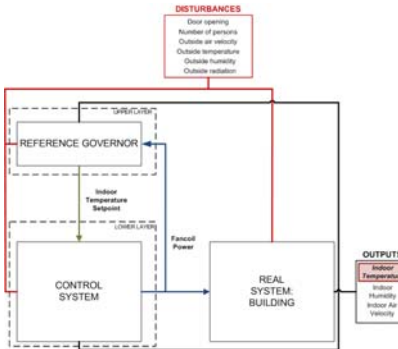


## Linear controllers for users' thermal comfort



**A hierarchical predictive control strategy**

- This structure is based on a traditional control scheme with a reference governor in a top layer, that by means of a nonlinear optimizer is able to generate an indoor temperature reference.



$$\Delta w_T = \min_{\Delta w_T} J_{k(1,2)}$$


$$J_{k1} = \sum_{j=1}^N \hat{y}_{PMV}(k+j|k)^2 + \lambda \sum_{j=1}^{N_u} \Delta w_T(k+j-1)^2$$

$$J_{k2} = \sum_{j=1}^N \hat{y}_{PMV}(k+j|k)^2 + \lambda \sum_{j=1}^{N_u} \Delta u(k+j-1)^2$$


$$w_{T \min} \leq w_T(k+j-1) \leq w_{T \max} \quad \forall j = 1, \dots, N_u$$

$$u_{\min} \leq u(k+j-1) \leq u_{\max} \quad \forall j = 1, \dots, N_u$$

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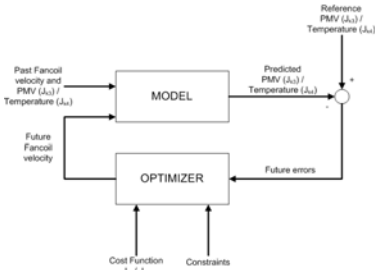


## Linear controllers for users' thermal comfort



### A classical MPC strategy

- This technique uses a model of the system to make predictions of the future outputs. They are included inside a cost function which establishes a relationship between the close loop behaviour of the system and the control effort. This cost function is minimized taking into account the constraints of the problem. Finally, a receding horizon strategy is implemented.




$$\Delta u = \min_{\Delta u} J_{k[3,4]}$$

$$J_{k3} = \sum_{j=1}^N \hat{y}_{PMV}(k+j|k)^2 + \lambda \sum_{j=1}^{N_u} \Delta u(k+j-1)^2$$


$$J_{k4} = \sum_{j=1}^N (\hat{y}_T(k+j|k) - w_T(k+j))^2 + \lambda \sum_{j=1}^{N_u} \Delta u(k+j-1)^2$$

$w_T \min \leq w_T(k+j-1) \leq w_T \max \quad \forall j = 1, \dots, N_u$ 
 $u_{\min} \leq u(k+j-1) \leq u_{\max} \quad \forall j = 1, \dots, N_u$

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## Linear controllers for users' thermal comfort

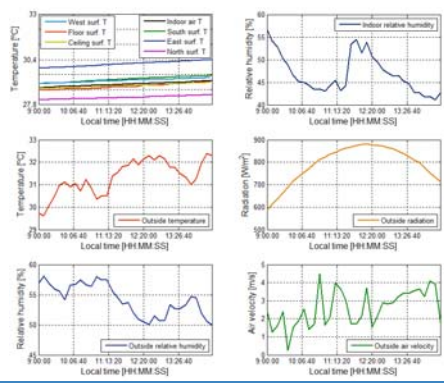


### Selection of weighting coefficients for the cost functions

- It is almost impossible to find different days with identical conditions, since these variables are non controllable. Thus, a typical day for the analyzed period has been chosen to compare different strategies through simulations.

Strategy	Lambda ( $\lambda$ )	ISE Criterion
(A): $J_{k1}$	0.1	20.01
	0.3	33.46
(B): $J_{k2}$	0.0065	27.29
	0.008	33.37
(C): $J_{k3}$	0.001	19.77
	0.00355	33.53
(D): $J_{k4}$	0.012	27.83
	0.2	58.53

$$ISE = \int_0^{\infty} e(t)^2 dt$$



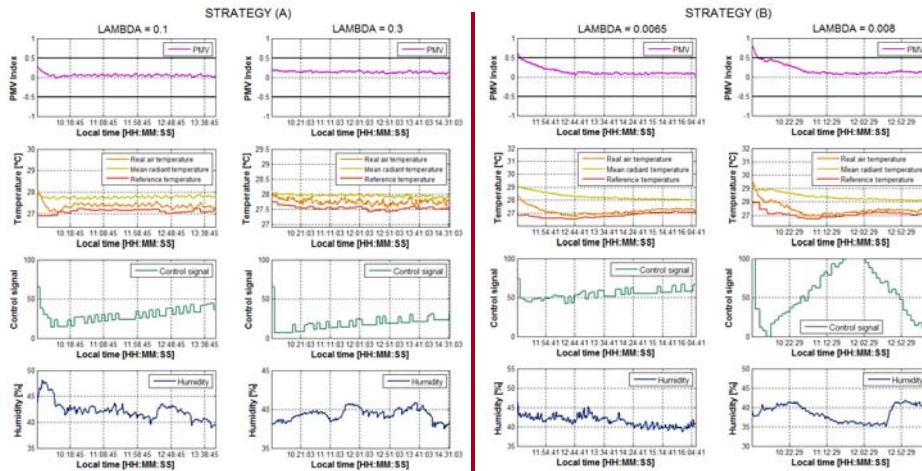
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## Linear controllers for users' thermal comfort



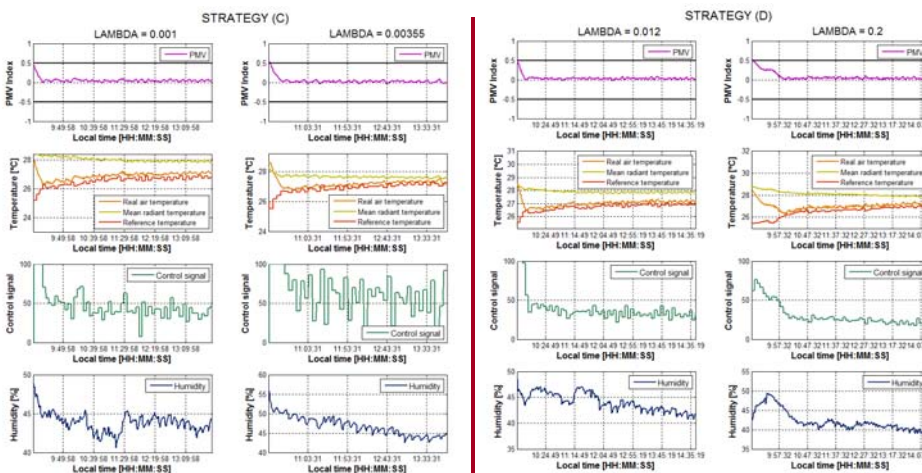
### Results from the hierarchical predictive control strategy




## Linear controllers for users' thermal comfort




### Results from the classical MPC strategy



75



## Linear controllers for users' thermal comfort



**Results**


- A comparison among different strategies have been performed as a function of several indexes:
  - Index 1: Mean number of changes per hour [-].
  - Index 2: Percentage of total time in which the HVAC system is connected [%].
  - Index 3: Average energy consumption per hour [W].

Strategy	Lambda ( $\lambda$ )	ISE Criterion	Index 1	Index 2	Index 3
(A): $J_{k1}$	0.1	20.01	30	30.13	40
	0.3	33.46	62	18.20	24
(B): $J_{k2}$	0.0065	27.29	58	42.50	56
	0.008	33.37	84	37.74	50
(C): $J_{k3}$	0.001	19.77	42	42.14	55
	0.00355	33.53	35	29.39	39
(D): $J_{k4}$	0.012	27.83	47	33.26	44
	0.2	58.53	57	41.61	55


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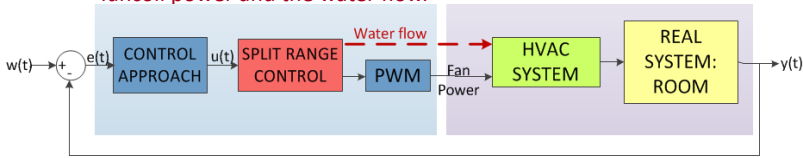
76

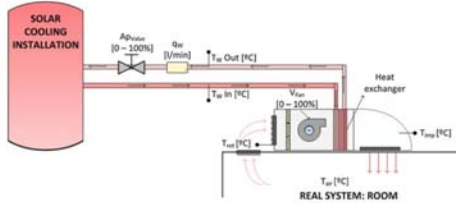


## A nonlinear controller for users' thermal comfort

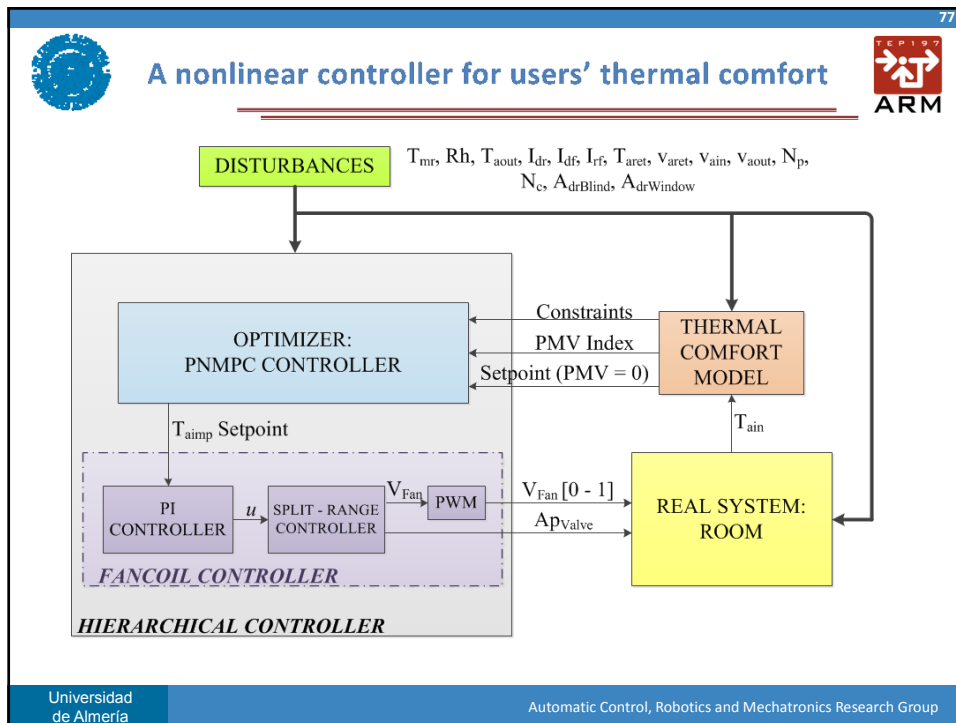


- **Main objective.** To obtain a high thermal comfort level trying to reduce energy consumption.
- Main differences of this approach with the linear control approaches:
  - The use of a nonlinear first principles model which accurately reflects the dynamics of the room climate and takes into account the main disturbances.
  - It has been considered that the HVAC system has two degrees of freedom, the fancoil power and the water flow.





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78

**A nonlinear controller for users' thermal comfort**

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**Optimization layer: A nonlinear MPC approach**

- In general, MPC control algorithms, as Generalized Predictive Control (GPC), are applied to linear systems that are characterized by the use of a predicted output data vector,  $\hat{Y}$ , throughout a prediction horizon,  $N$ , as a function of a vector which contains changes in the control action,  $\Delta u$ :
 
$$\hat{Y} = F + G \cdot \Delta u$$
 where the system free response vector,  $F$ , and the matrix  $G$  are estimated by means of different methods depending of the selected algorithm.
- In this case, the PNMPC strategy is used to compute both  $F$  and  $G$  from the non-linear model explained previously.
 
$$\hat{Y} = F + G_{PNMPC} \cdot \Delta u$$


$$F = f(y_p, \Delta u_p, \Delta v_p) \quad G_{PNMPC} = \frac{\partial \hat{Y}}{\partial \Delta u}$$

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79



## Thermal comfort control inside a room



**A Practical Non-Linear Model Predictive Control (PNMPC) approach**


$$\hat{Y} = F + G_{PNMPC} \cdot \Delta u$$

$$F = f(y_p, \Delta u_p, \Delta v_p) \quad G_{PNMPC} = \frac{\partial \hat{Y}}{\partial \Delta u}$$


$$G = \begin{bmatrix} \frac{\partial \bar{y}(k+1)}{\partial \Delta u(k)} & 0 & \dots & 0 \\ \frac{\partial \bar{y}(k+2)}{\partial \Delta u(k)} & \frac{\partial \bar{y}(k+2)}{\partial \Delta u(k+1)} & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial \bar{y}(k+N_2)}{\partial \Delta u(k)} & \frac{\partial \bar{y}(k+N_2)}{\partial \Delta u(k+1)} & \dots & \frac{\partial \bar{y}(k+N_2)}{\partial \Delta u(k+N_u-1)} \end{bmatrix}$$

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80



## Thermal comfort control inside a room



**A Practical Non-Linear Model Predictive Control (PNMPC) approach**

- The control law is obtained using techniques similar to the used in classical MPC algorithms.
 

$$\hat{Y} = F + G_{PNMPC} \cdot \Delta u$$

$$F = f(y_p, \Delta u_p, \Delta v_p) \quad G_{PNMPC} = \frac{\partial \hat{Y}}{\partial \Delta u}$$


  - Cost function
 
$$J = \sum_{j=1}^N \delta(j) [\hat{Y}(k+j|k) - w(k+j|k)]^2 + \sum_{j=1}^{N_u} \lambda(j) [u(k+j-1)]^2$$
  - Constraints
 
$$\Delta u_{\min} \leq \Delta u(k+j|k) \leq \Delta u_{\max} \quad \forall j = 0, \dots, N_u - 1$$

$$u_{\min} \leq u(k+j|k) \leq u_{\max} \quad \forall j = 0, \dots, N_u - 1$$


$$\hat{Y}_{\min} \leq \hat{Y}(k+j|k) \leq \hat{Y}_{\max} \quad \forall j = 0, \dots, N - 1$$

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## Thermal comfort control inside a room




A Practical Non-Linear Model Predictive Control (PNMPC) approach


- To estimate  $F$  and  $G_{PNMPC}$  at each sample time it is necessary to use the following algorithm:
  - 1. Obtain  $\hat{Y}^0$  vector with a length of  $N$ . To do that, it is necessary to execute the model using past inputs, outputs and measurable disturbances, and with  $\Delta u = [0 \ 0 \ \dots \ 0]^T$ .
 
$$\hat{Y}^0 = F$$
  - 2. Estimate the first column of the  $G_{PNMPC}$  matrix. The model has to be executed using past inputs, outputs and measurable disturbances, and, in this case, with  $\Delta u = [\epsilon \ 0 \ \dots \ 0]^T$  where  $\epsilon$  is a very small value, such as,  $u(k-1)/1000$ .
 
$$G_{PNMPC}(:,1) = (\hat{Y}^1 - \hat{Y}^0) / \epsilon$$
  - 3. Estimate the second column of the  $G_{PNMPC}$  matrix. The model has to be executed using past inputs, outputs and measurable disturbances, and, in this case, with  $\Delta u = [0 \ \epsilon \ \dots \ 0]^T$ .
 
$$G_{PNMPC}(:,2) = (\hat{Y}^2 - \hat{Y}^0) / \epsilon$$
  - 4. Continue with the remainder columns of  $G_{PNMPC}$  matrix until the last column where  $Y^{Nu}$  vector is obtained executing the model with past inputs and outputs, and with  $\Delta u = [0 \ 0 \ \dots \ \epsilon]^T$  where  $Nu$  is the control horizon.
 
$$G_{PNMPC}(:,Nu) = (\hat{Y}^{Nu} - \hat{Y}^0) / \epsilon$$

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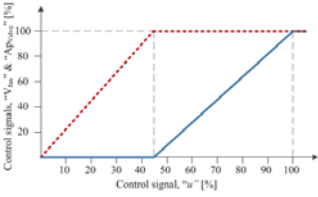
## A nonlinear controller for users' thermal comfort



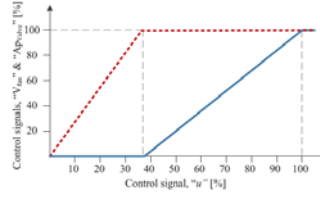
Control layer: Fancoil MISO Controller

- The fancoil unit available in the CDdI-CIESOL-ARFRISOL building allows to change the impulse air temperature by the regulation of the water flow through it, and/or the return air velocity.
- To do that, a discrete PI with antiwindup combined with a split-range control strategy has been used.

Winter

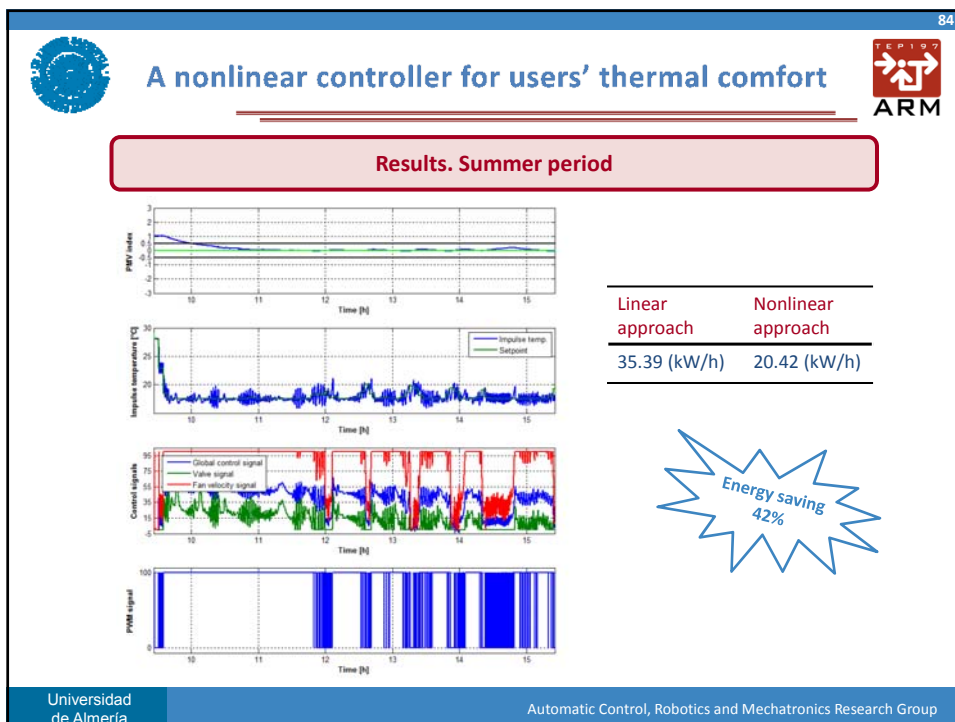
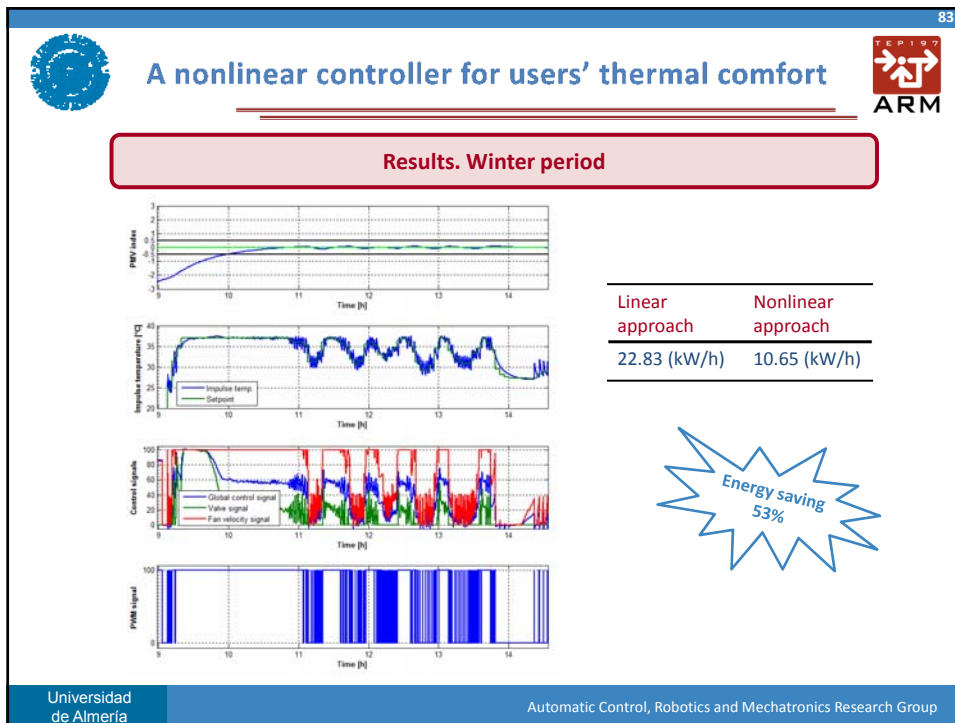


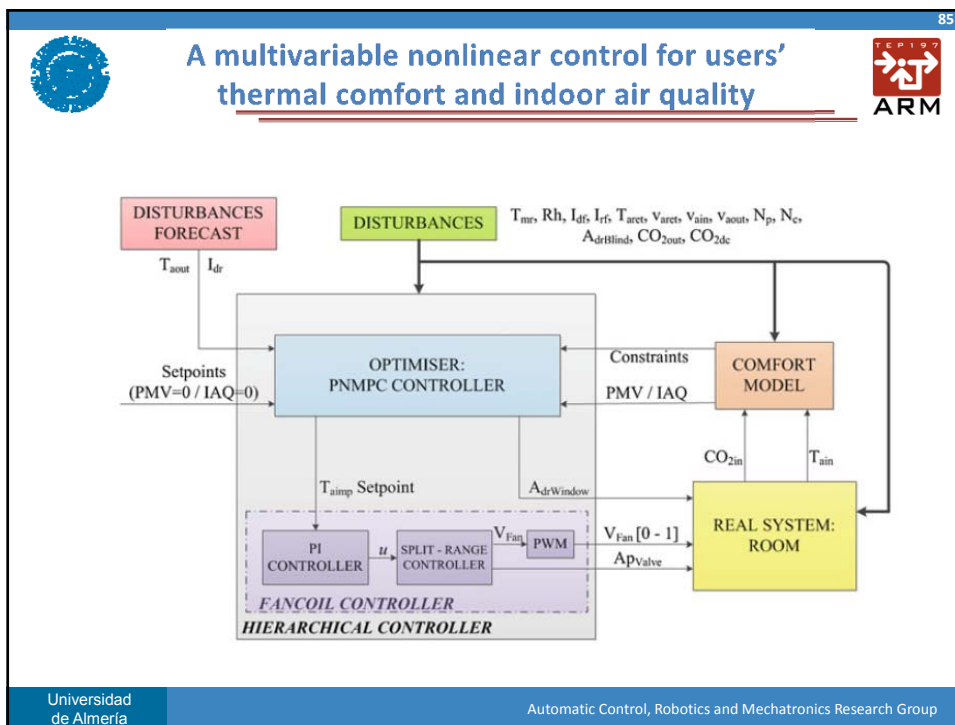
Summer



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86

**A multivariable nonlinear MPC approach**

- In this case, for the multivariable approach:
 
$$\begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \end{bmatrix} = \begin{bmatrix} f_1 \\ f_2 \end{bmatrix} + G_{PNMPC} \begin{bmatrix} \Delta u_1 \\ \Delta u_2 \end{bmatrix}$$

$$\hat{y} = f + G \Delta u$$

$$f_i = f(y_{ip}, \Delta u_{jp}, \Delta v_p)$$

$$G_{PNMPC} = \begin{bmatrix} \frac{\partial \hat{y}_1}{\partial \Delta u_1} & \frac{\partial \hat{y}_1}{\partial \Delta u_2} \\ \frac{\partial \hat{y}_2}{\partial \Delta u_1} & \frac{\partial \hat{y}_2}{\partial \Delta u_2} \end{bmatrix}$$

$$J = \sum_{i=1}^2 \sum_{j=1}^N \delta_i [\hat{y}_i(k+j|k) - w_i(k+j)]^2 + \sum_{c=1}^2 \sum_{j=1}^{N_u} \lambda_c [\Delta u_c(k+j-1)]^2$$

$$G = \begin{bmatrix} G_{1,1} & G_{1,2} \\ G_{2,1} & G_{2,2} \end{bmatrix}$$

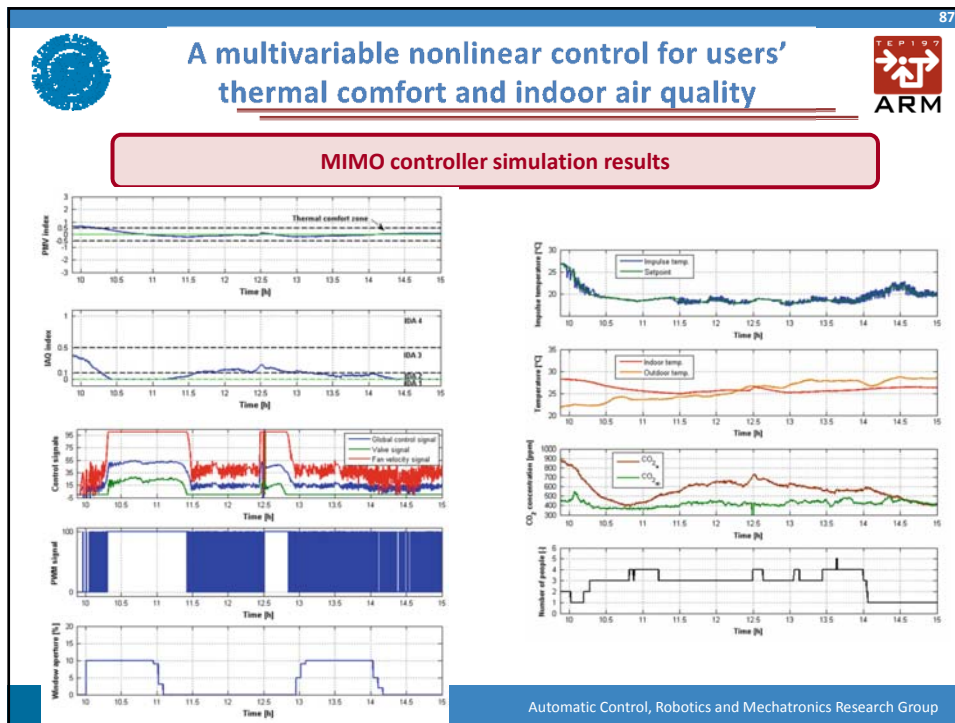
$$\Delta u = \begin{bmatrix} \Delta u_1 \\ \Delta u_2 \end{bmatrix}$$

$$\begin{bmatrix} \Delta u_{1min} \\ \Delta u_{2min} \end{bmatrix} \leq \begin{bmatrix} \Delta u_1(k+j-1) \\ \Delta u_2(k+j-1) \end{bmatrix} \leq \begin{bmatrix} \Delta u_{1max} \\ \Delta u_{2max} \end{bmatrix} \quad \forall j = 1, \dots, N_u$$


$$\begin{bmatrix} u_{1min} \\ u_{2min} \end{bmatrix} \leq \begin{bmatrix} u_1(k+j-1) \\ u_2(k+j-1) \end{bmatrix} \leq \begin{bmatrix} u_{1max} \\ u_{2max} \end{bmatrix} \quad \forall j = 1, \dots, N_u.$$

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88



## Index




- Motivation and main objectives
- The CIESOL building
- Comfort in buildings
  - Predicted Mean Vote (PMV) index
  - PMV index approximations
- Thermal comfort control inside a room
  - Linear Predictive Control
  - First principles model of a room
  - A Practical Non-Linear Model Predictive Control (PNMPC) approach
- Actual works


Actual works

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89

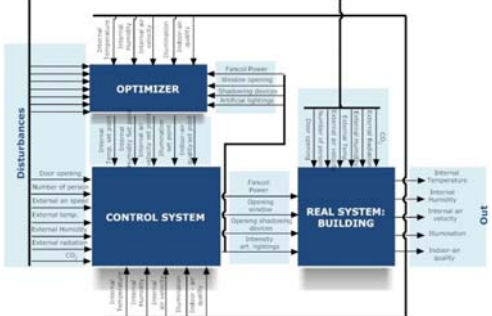


## Actual works



- Simplified modeling efforts
- Perform real tests of PNMPC approach in the building.
- Develop a distributed MPC controller.
- Obtain luminance and CO<sub>2</sub> concentration models for a typical room of the building.
- Develop a MIMO MPC/hierarchical controller in order to maintain users' comfort.


MIMO controller architecture




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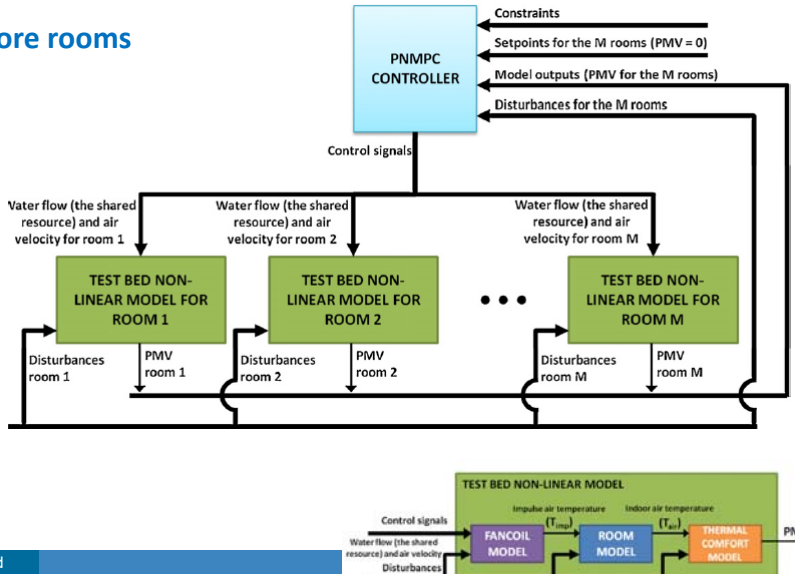
90




## Actual works




### More rooms



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## Actual works



### More rooms

$$\sum_{i=1}^M u_i(t + j|t) \leq a, \quad \forall j = 1, \dots, N$$

$$\sum_{i=1}^M \dot{q}_{wi} \leq 60 \text{ l/min},$$

$$N_i = 10 \quad N_{u_i} = 4$$

$P(k) : \min J(\Delta \mathbf{u}) = \frac{1}{2} \Delta \mathbf{u}^T \mathbf{H} \Delta \mathbf{u} + \mathbf{b}^T \Delta \mathbf{u} + f_0$

s.to :  $\mathbf{A} \mathbf{u} \leq \mathbf{a}$

$\Delta \mathbf{u}_{\min} \leq \Delta \mathbf{u} \leq \Delta \mathbf{u}_{\max}$

$\mathbf{u}_{\min} \leq \mathbf{u} \leq \mathbf{u}_{\max}$

$\hat{\mathbf{y}}_{\min} \leq \hat{\mathbf{y}} \leq \hat{\mathbf{y}}_{\max}$

$-1 \text{ l/min} \leq \Delta \dot{q}_{wi} \leq 1 \text{ l/min}$

$2 \text{ l/min} \leq \dot{q}_{wi} \leq 25 \text{ l/min}$


$0.2 \text{ m/s} \leq V_{Fan_i} \leq 1.5 \text{ m/s}$

$-0.1 \text{ l/min} \leq \Delta V_{Fan_i} \leq 0.1 \text{ l/min}$


$4\lambda_{vi} = \lambda_{qi}$

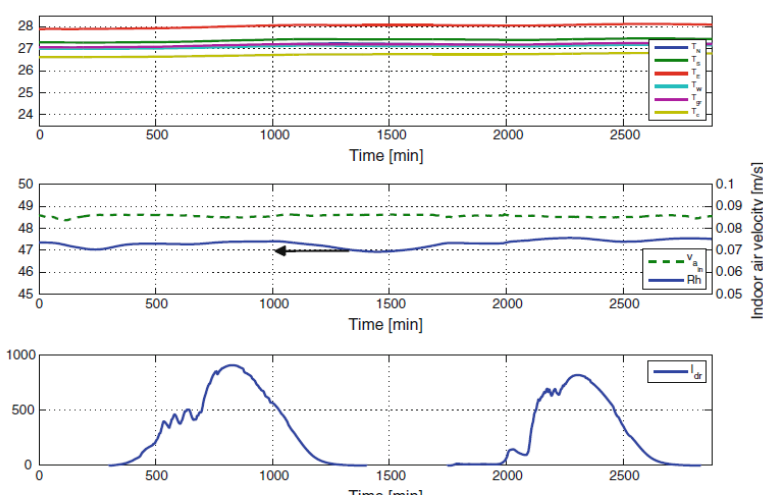
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## Actual works





**Fig. 5.41** Boundary conditions in the simulations. From top to bottom, first graph radiant temperatures (North, South, East, West, ceiling and ground), second graph indoor air velocity and indoor air humidity, and third graph direct solar irradiation (Álvarez et al. 2013)

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95



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